

Roll No. _____

MATHEMATICS
Time: 30 Minutes

Intermediate Part-I, Class 11th (1stA 324-IV) PAPER: I GROUP: II
OBJECTIVE
Code: 6198 *GUJ-2-24*
Marks: 20

Note: You have four choices for each objective type question as A, B, C and D. The choice which you think is correct, fill that circle in front of that question number. Use marker or pen to fill the circles. Cutting or filling two or more circles will result in zero mark in that question.

- 1- 1- a, b and c are in A.P, then
(A) $2a = b - c$ (B) $2b = a + c$ (C) $2b = a - c$ (D) $2a = b + c$
- 2- Number of terms in expansion of $(1 + x)^{n-1}$ is
(A) $n + 2$ (B) $n + 1$ (C) n (D) $n - 1$
- 3- H is Harmonic mean between a and b then $H =$ _____
(A) $\frac{2ab}{a+b}$ (B) $\frac{a+b}{2ab}$ (C) $\frac{2ab}{a-b}$ (D) $\frac{a-b}{2ab}$
- 4- $\cos(\tan^{-1}0) =$ _____
(A) 0 (B) 1 (C) -1 (D) ∞
- 5- In $\frac{p(x)}{q(x)}$, degree of p(x) is less than degree of q(x), then fraction is
(A) proper (B) improper (C) combined (D) partial
- 6- Set having no proper subset
(A) $\{ \}$ (B) $\{ 1 \}$ (C) $\{ 1, 2 \}$ (D) $\{ 1, 2, 3 \}$
- 7- Recurring decimal is a _____ number.
(A) prime (B) rational (C) irrational (D) integer
- 8- Sum of roots of equation $x^2 - 5x + 6 = 0$
(A) 6 (B) -6 (C) 5 (D) -5
- 9- ${}^nC_8 = {}^nC_{12}$, then value of n is
(A) 8 (B) 12 (C) 16 (D) 20
- 10- Proposition _____ is called biconditional
(A) $p \rightarrow q$ (B) $p \leftrightarrow q$ (C) $p \wedge q$ (D) $p \vee q$
- 11- $\sin x = \frac{1}{2}$, then $x =$ _____
(A) $\frac{\pi}{6}$ (B) $\frac{\pi}{4}$ (C) $\frac{\pi}{3}$ (D) $\frac{\pi}{2}$
- 12- Number of radians in semi-circle
(A) $\frac{\pi}{2}$ (B) π (C) 2π (D) $\frac{2\pi}{3}$
- 13- $3^{2x} + 4 \cdot 3^x + 4 = 0$ is _____ equation.
(A) cubic (B) radical (C) reciprocal (D) exponential
- 14- Period of $\tan x$ is
(A) $\frac{\pi}{2}$ (B) 3π (C) 2π (D) π
- 15- $(-1)^{-\frac{21}{2}} = \dots\dots$
(A) 1 (B) -1 (C) i (D) -i
- 16- If $\begin{bmatrix} x & 1 \\ 3 & 1 \end{bmatrix}$ is singular, then $x =$ _____
(A) -3 (B) 3 (C) 1 (D) -1
- 17- Sum of opposite angles of cyclic quadrilateral is
(A) 90 (B) 120 (C) 180 (D) 270
- 18- The matrix $\begin{bmatrix} 1 & 2 & 3 \end{bmatrix}$ is _____ matrix.
(A) square (B) unit (C) null (D) row
- 19- Co-ratio of Cosine is
(A) sine (B) cosine (C) tangent (D) secant
- 20- If $A = \{1, 2, 3\}$ and $B = \{4, 5\}$, which is not element of $A \times B$
(A) (1, 4) (B) (2, 4) (C) (3, 4) (D) (4, 3)

Note: Section-I is compulsory. Attempt any three (3) questions from Section-II.

SECTION-I

2. Write short answers to any EIGHT questions:

(2 x 8 = 16)

- i- Write trichotomy and transitive properties of inequalities of real numbers.
- ii- Simplify $(2, 6) \div (3, 7)$
- iii- Find the modulus of $3 + 4i$
- iv- Express the complex number $1 + i\sqrt{3}$ in polar form
- v- Write inverse, converse and contrapositive of the conditional $\sim p \rightarrow \sim q$
- vi- Define groupoid.
- vii- If $A = \begin{bmatrix} i & 0 \\ 1 & -i \end{bmatrix}$, show that $A^4 = I_2$

viii- Without expansion verify that $\begin{vmatrix} \alpha & \beta + \gamma & 1 \\ \beta & \gamma + \alpha & 1 \\ \gamma & \alpha + \beta & 1 \end{vmatrix} = 0$

- ix- If A and B are non-singular matrices, then show that $(AB)^{-1} = B^{-1}A^{-1}$
- x- Find the three cube roots of -27
- xi- Use the factor theorem to determine if $x - 1$ is a factor of $x^2 + 4x - 5$
- xii- If α, β are the roots of $3x^2 - 2x + 4 = 0$, find the value of $\frac{1}{\alpha^2} + \frac{1}{\beta^2}$

3. Write short answers to any EIGHT questions:

(2 x 8 = 16)

- i- Resolve into Partial Fractions $\frac{3x}{(x-1)(x+2)}$
- ii- Define the term Partial Fraction.
- iii- Write the first four terms of the sequence, if $a_n - a_{n-1} = n + 2$, $a_1 = 2$
- iv- If 5, 8 are two A.Ms between a and b, find a and b.
- v- Find the sum of infinite Geometric Series $\frac{9}{4} + \frac{3}{2} + 1 + \frac{2}{3} + \dots$
- vi- Find the 8th term of H.P; $\frac{1}{2}, \frac{1}{5}, \frac{1}{8}, \dots$
- vii- Prove that ${}^nC_r = {}^nC_{n-r}$
- viii- Find the value of n when ${}^{11}P_n = 11.10.9$
- ix- What is the probability that a slip of numbers divisible by 4 are picked from the slips bearing numbers 1, 2, 3, ..., 10?
- x- Prove that the inequality $n^2 > n + 3$ for $n = 3, 4$
- xi- Calculate $(9.9)^5$ by means of Binomial Theorem.
- xii- Expand $(1 - x)^{1/2}$ upto 4 terms.

4. Write short answers to any NINE questions:

(2 x 9 = 18)

- i- Find r when $\ell = 5\text{cm}$, $\theta = \frac{1}{2}$ radian
- ii- Evaluate $\frac{\tan \frac{\pi}{3} - \tan \frac{\pi}{6}}{1 + \tan \frac{\pi}{3} \cdot \tan \frac{\pi}{6}}$
- iii- Prove that $\sin(\alpha + \beta) \sin(\alpha - \beta) = \cos^2 \beta - \cos^2 \alpha$

(Turn Over)

(2)

- iv- Prove that $\frac{\cos 8^\circ - \sin 8^\circ}{\cos 8^\circ + \sin 8^\circ} = \tan 37^\circ$
- v- Express as product : $\cos 7\theta - \cos \theta$
- vi- Define Periodicity.
- vii- Find period of $3\cos \frac{x}{5}$
- viii- Draw graph of $\sin x$ when $x \in [0, \pi]$
- ix- Find a and c for the right angle triangle ABC, when $\alpha = 58^\circ 13'$, $b = 125.7$, $\gamma = 90^\circ$
- x- A vertical pole is 8m high and length of its shadow is 6m. What is angle of elevation of the sun at that moment?
- xi- Solve the triangle ABC if $b = 125$, $\gamma = 53^\circ$, $\alpha = 47^\circ$
- xii- Show that $\tan(\sin^{-1} x) = \frac{x}{\sqrt{1-x^2}}$
- xiii- Solve the trigonometric equation $\sin x = -\frac{\sqrt{3}}{2}$

SECTION-II

- 5- (a) Solve the system of linear equations by Cramer's Rule : 5
- $$\begin{aligned} 2x + 2y + z &= 3 \\ 3x - 2y - 2z &= 1 \\ 5x + y - 3z &= 2 \end{aligned}$$
- (b) Show that the roots of $(mx + c)^2 = 4ax$ will be equal if $c = \frac{a}{m}$, $m \neq 0$ 5
- 6- (a) Resolve $\frac{x^2 + x - 1}{(x+2)^3}$ into partial fractions. 5
- (b) The sum of an infinite Geometric Series is 9 and the sum of the squares of its terms is $\frac{81}{5}$. 5
- Find the series.
- 7- (a) Two dice are thrown. E_1 is the event that the sum of their dots is an odd number and E_2 is the event that 1 is the dot on the top of the first die. Show that $P(E_1 \cap E_2) = P(E_1) \cdot P(E_2)$ 5
- (b) Find the term independent of x in expansion of $\left(\sqrt{x} + \frac{1}{2x^2}\right)^{10}$ 5
- 8- (a) Prove that $\sin \frac{\pi}{9} \sin \frac{2\pi}{9} \sin \frac{\pi}{3} \sin \frac{4\pi}{9} = \frac{3}{16}$ 5
- (b) Show that $r_2 = 4R \cos \frac{\alpha}{2} \sin \frac{\beta}{2} \cos \frac{\gamma}{2}$ 5
- 9- (a) Find x if $\tan^2 45^\circ - \cos^2 60^\circ = x \sin 45^\circ \cos 45^\circ \tan 60^\circ$ 5
- (b) Prove that $\sin^{-1} \frac{4}{5} + \sin^{-1} \frac{5}{13} + \sin^{-1} \frac{16}{65} = \frac{\pi}{2}$ 5