Inter. (Part-I)-A- 2021

Roll No._____to be filled in by the candidate. (For all sessions) | Paper Code | 6 | 1 | 9 | 1 |

Mathematics (Objective Type)

Time: 30 Minutes Marks: 20

NOTE: Write answers to the questions on objective answer sheet provided. Four possible answers A,B,C & D to each question are given. Which answer you consider correct, fill the corresponding circle A,B,C or D given in front of each question with Marker or pen ink on the answer sheet provided.

1-1. Multiplicative identity of complex number is:

(A) (0,0) (B) (0,1) (C) (1,0) (D) (1,1)

2. The contrapositive of $\sim p \rightarrow \sim q$ is:

(A) $p \rightarrow q$ (B) $q \rightarrow p$ (C) $\sim q \rightarrow \sim p$ (D) $\sim q \rightarrow p$

3. If A and B are any two non singular matrices then $(AB)^{-1} =$

(A) $A^{-1}B^{-1}$ (B) $B^{-1}A^{-1}$ (C) BA (D) AB

4. For a non-singular matrix A if $XA=B$ then $X =$

(A) $A^{-1}B$ (B) BA^{-1} (C) $(AB)^{-1}$ (D) $(BA)^{-1}$

5. If $f(x)=3x^4+4x^3+x-5$ is divided by $x+1$, then remainder is:

(A) -6 (B) 7 (C) 6 (D) -7

6. If w is cue root of unity, then $w^{15}=$

(A) 1 (B) 0 (C) w (D) -w

7. Partial fraction of $\frac{3x-11}{(x^2+1)(x+3)}$ will be of the form:

(A) $\frac{Ax+B}{x^2+1}+\frac{C}{x+3}$ (B) $\frac{A}{x^2+1}+\frac{Bx+C}{x+3}$ (C) $\frac{Ax+B}{x+3}+\frac{C}{x^2+1}$ (D) $\frac{A}{x^2+1}+\frac{B}{x+3}$

8. If $a_n=(-1)^{n+1}$, then 26^{th} term is:

(A) 1 (B) -1 (C) 26 (D) -26

9. $(n+1)^{th}$ term of G.P is:

(A) $a_1 r^{n-1}$ (B) $a_1 r^{n+1}$ (C) $a_1 r^{n+2}$ (D) $a_1 r^n$

10. n^{th} term of A.P is:

(A) $a_1+(n-1)d$ (B) $a_1+(n+1)d$ (C) $2a_1+(n-1)d$ (D) $a_1+(2n-1)d$

11. With usual notation $^nC_r + {}^nC_{r-1} =$

(A) $^nC_{r+1}$ (B) $^{n+1}C_r$ (C) $^{n-1}C_{r-1}$ (D) $^{n+1}C_{r-1}$

12. In the expansion of $(a+b)^7$, the second term is:

(A) a^7 (B) $7a^6b$ (C) $7ab^6$ (D) 8

13. In one hour, the hour hand of a clock turns through an angle.

(A) $\frac{\pi}{8}$ (B) $\frac{\pi}{4}$ (C) $\frac{\pi}{6}$ (D) $\frac{\pi}{2}$

14. $3\frac{\pi}{4}$ radian is equal to:

(A) 110^0 (B) 135^0 (C) 150^0 (D) 130^0

15. $\sin(-300^0) =$

(A) $-\frac{\sqrt{3}}{2}$ (B) $\frac{\sqrt{3}}{2}$ (C) $\frac{1}{2}$ (D) 0

16. Period of $\sin x$ is:

(A) π (B) 2π (C) 3π (D) $-\pi$

17. Radius of escribed circle opposite to vertex C is:

(A) $\frac{\Delta}{s-a}$ (B) $\frac{\Delta}{s-b}$ (C) $\frac{\Delta}{s-c}$ (D) $\frac{\Delta}{s}$

18. With usual notation $a+b-c =$

(A) $2S$ (B) $2S-2C$ (C) $2S-2b$ (D) $2S-c$

19. $2\tan^{-1}A =$

(A) $\tan^{-1}\frac{2A}{1-A^2}$ (B) $\tan^{-1}\frac{2A}{1+A^2}$ (C) $\tan^{-1}\frac{A}{1-A^2}$ (D) $\tan^{-1}\frac{A}{1+A^2}$

20. Solution of $\cot\theta=\frac{1}{\sqrt{3}}$ in quadrant III is:

(A) $\frac{5\pi}{3}$ (B) $7\frac{\pi}{6}$ (C) $\frac{4\pi}{3}$ (D) $\frac{7\pi}{3}$

821-11-A-☆

Inter - (Part-I) -A-2021

Roll No._____ *to be filled in by the candidate.*

(For all sessions)

Mathematics (Essay Type)

Time: 2:30 Hours RwP-21 **Marks: 80**

Section -I

2. Write short answers of any eight parts from the following. **2x8=16**

i. Seperate into real and imaginary parts $\frac{2-7i}{4+5i}$.

ii. Factorize $3x^2+3y^2$.

iii. Simplify $(2,6)(3,7)$.

iv. Let $A=\{1,2,3,4\}$, Find the relation $\{(x,y)/x+y<5\}$ in A

v. Write the inverse and converse of $\sim p \rightarrow \sim q$

vi. Find the value of x if $\begin{vmatrix} 3 & 1 & x \\ -1 & 3 & 4 \\ x & 1 & 0 \end{vmatrix} = -30$

vii. Find the condition that one root of $x^2+px+q=0$ is multiplicative inverse of other.

viii. Evaluate $\left(1+w+w^2\right)\left(1-w+w^2\right)$.

ix. Solve the equation $ax=b$ where a,b are the elements of a group G

x. Discuss the nature of roots of the equation $2x^2-5x+1=0$.

xi. If $A=\begin{bmatrix} 1 & 2 \\ a & b \end{bmatrix}$ and $A^2=\begin{bmatrix} 0 & 0 \\ 0 & 0 \end{bmatrix}$ then find the values of a and b.

xii. If A and B are square matrices of the same order, then explain why in general $(A+B)(A-B) \neq A^2-B^2$.

3. Write short answers of any eight parts from the following. **2x8=16**

i. Which term of the A.P, -2,4,10,.....is 148?

ii. Insert three G.M's between 1 and 16.

iii. Write in factorial form $\frac{(n+1)(n)(n-1)}{3.2.1}$.

iv. Find the value of n, when ${}^{n}P_4 : {}^{n-1}P_3 = 9:1$

v. If 5 is the harmonic mean between 2 and b, find b.

vi. Find the number of diagonals of a 6-sided figure.

vii. Evaluate $\sqrt[3]{30}$ correct to two places of decimals.

viii. Expand by binomial theorem $\left(\sqrt{\frac{a}{x}}-\sqrt{\frac{x}{a}}\right)^3$.

ix. Resolve into partial fractions $\frac{7x+25}{(x+3)(x+4)}$.

x. Resolve into partial fractions without finding the constants $\frac{9x-7}{(x^2+1)(x+3)}$

xi. If $\frac{1}{a}, \frac{1}{b}$ and $\frac{1}{c}$ are in G.P, show that the common ratio is $\pm\sqrt{\frac{a}{c}}$.

xii. Check whether, $1+\frac{1}{2}+\frac{1}{4}+.....+\frac{1}{2^{n-1}}=2\left(1-\frac{1}{2^n}\right)$ is true for $n=1,2$.

Rwp-21

4. Write short answers of any nine parts from the following. **2x9=18**

i. Prove that $\sec^2\theta - \operatorname{cosec}^2\theta = \tan^2\theta - \cot^2\theta$.

ii. Find the values of $\cos 105^0$ taking $(105^0 = 45^0 + 60^0)$.

iii. Prove that $\frac{\sin 8x + \sin 2x}{\cos 8x + \cos 2x} = \tan(5x)$.

iv. Find the period of $\tan(4x)$.

v. Show that $\gamma = (s-c)\tan\left(\frac{\gamma}{2}\right)$.

vi. In ΔABC a=3,b=6 and B=36^{0}20' Find "b".

vii. Find area of ΔABC if a=18, b=24 and c=30.

viii. Find the value of $\cos^{-1}\left(\frac{-1}{2}\right)$.

ix. Solve the equation $1+\cos x = 0$.

x. Find the soln of equation $\sec x = -2$ which lies in $[0, 2\pi]$.

xi. What is the circular measure of the angle between the hands of a watch at 4 'o' clock.

xii. Find the values of remaining trigonometric functions when $\cos\theta = \frac{9}{41}$ and the terminal arm of the angle is in quad Iv

xiii. If α, β and γ are angles of a triangle ABC then prove that $\tan(\alpha+\beta) + \tan\gamma = 0$.

Section -II

Note: Attempt any three questions from the following. **10x3=30**

5. (a) If $A = \begin{bmatrix} 2 & -1 \\ 3 & 1 \end{bmatrix}$ verify that $(A^{-1})^t = (A^t)^{-1}$.

(b) Solve the system of equations $x + y = 5$; $\frac{2}{x} + \frac{3}{y} = 2$.

6. (a) Resolve $\frac{1}{(1-ax)(1-bx)(1-cx)}$ into partial fractions.

(b) For what value of n, $\frac{a^n + b^n}{a^{n-1} + b^{n-1}}$ is the positive Geometric Meam (G.M) between a and b.

7. (a) Prove that $C_r^n + C_{r-1}^n = C_r^{n+1}$.

(b) If x is so small that its cube and higher powers can be neglected then show that $\sqrt{\frac{1+x}{1-x}} \approx 1 + x + \frac{1}{2}x^2$.

8. (a) Two cities A and B lie on the equator such that their longitudes are 45^{0}E and 25^{0}W respectively. Find the distance between two cities, taking radius of earth as 6400 kms.

(b) Show that $\cos(\alpha+\beta)\cos(\alpha-\beta) = \cos^2\alpha - \sin^2\beta = \cos^2\beta - \sin^2\alpha$.

9. (a) The sides of a triangle are $x^2+x+1, 2x+1$ and x^2-1. Prove that the greatest angle of the triangle is 120^0.

(b) Prove that $2\tan^{-1}\left(\frac{1}{3}\right) + \tan^{-1}\left(\frac{1}{7}\right) = \frac{\pi}{4}$.