

Roll No _____ (To be filled in by the candidate)

(Academic Sessions 2019 – 2021 to 2021 – 2023)

MATHEMATICS

223-1st Annual-(INTER PART – II)

Time Allowed : 30 Minutes

Q.PAPER – II (Objective Type)

GROUP – II

Maximum Marks : 20

PAPER CODE = 8194 LHR-12-2-23

Note : Four possible answers A, B, C and D to each question are given. The choice which you think is correct, fill that circle in front of that question with Marker or Pen ink in the answer-book. Cutting or filling two or more circles will result in zero mark in that question.

1-1	The mid point of the line segment joining the foci of an ellipse is called : (A) Vertex (B) Directrix (C) Centre (D) Minor axis
2	If (3 , 5) is mid point of (5 , a) and (b , 7) then : (A) $a = 4, b = 2$ (B) $a = 3, b = 3$ (C) $a = 7, b = -2$ (D) $a = 3, b = 1$
3	If 2 and 2 are x and y components of a vector, then its angle with x-axis is : (A) 30° (B) 60° (C) 45° (D) 90°
4	(3 , 2) is not a solution of the inequality : (A) $x - y > 1$ (B) $x + y > 2$ (C) $3x + 5y > 8$ (D) $3x - 7y < 3$
5	$\underline{i} \times \underline{j} = :$ (A) \underline{k} (B) \underline{i} (C) \underline{j} (D) \underline{j}
6	Slope of line $3x - 2y + 5 = 0$ is : (A) $-\frac{2}{3}$ (B) $\frac{2}{3}$ (C) $\frac{3}{2}$ (D) $-\frac{3}{2}$
7	Length of the diameter of the circle $(x+5)^2 + (y-8)^2 = 12$: (A) $2\sqrt{3}$ (B) 12 (C) 24 (D) $4\sqrt{3}$
8	Transverse axis of the hyperbola $\frac{x^2}{a^2} - \frac{y^2}{b^2} = 1$ is : (A) $x = \frac{a}{e}$ (B) $y = 0$ (C) $x = 0$ (D) $y = \frac{a}{e}$
9	Equation of line in slope intercept form is : (A) $y = mx + c$ (B) $\frac{x}{a} + \frac{y}{b} = 1$ (C) $y - y_1 = m(x - x_1)$ (D) $x \cos \alpha + y \sin \alpha = p$
10	The condition for a line $y = mx + c$ to be tangent to the circle $x^2 + y^2 = a^2$ is that : (A) $c = \pm m\sqrt{1+a^2}$ (B) $c = \pm a\sqrt{1+m^2}$ (C) $c = \pm a\sqrt{1-m^2}$ (D) $c = \pm \sqrt{1-m^2}$

(Turn Over)

11	$f(x) = f(o) + xf'(o) + \frac{x^2}{2!} f''(o) + \frac{x^3}{3!} f'''(o) + \dots$ is called : (A) Taylor's series (B) Binomial series (C) Maclaurin's series (D) Laurent series
12	$\lim_{x \rightarrow 0} \frac{\sin 7x}{x} = :$ (A) 7 (B) -7 (C) $-\frac{1}{7}$ (D) $\frac{1}{7}$
13	$\int \frac{e^x}{e^x + 1} dx = :$ (A) $\ln(e^x + 1) + c$ (B) $\ln e^x + c$ (C) $e^{-x} + c$ (D) $e^x + c$
14	$\frac{d}{dx} (x^2 + 1)^2 = :$ (A) $2x(x^2 + 1)$ (B) $\frac{(x^2 + 1)^3}{3}$ (C) $2(x^2 + 1)$ (D) $4x(x^2 + 1)$
15	$\int \sin^2 x dx = :$ (A) $\frac{x}{2} - \frac{\sin 2x}{4} + c$ (B) $\frac{x}{2} + \frac{\sin 2x}{4} + c$ (C) $\frac{x}{2} - \frac{\sin 2x}{2} + c$ (D) $\frac{x}{2} + \frac{\sin 2x}{2} + c$
16	$\frac{d}{dx} (\tan x^2) = :$ (A) $\sec^2 x^2$ (B) $2x \sec^2 x^2$ (C) $-\sec^2 x^2$ (D) $-2x \sec x^2$
17	$\int e^x (\cos x - \sin x) dx = :$ (A) $e^x \sin x + c$ (B) $e^x \cos x + c$ (C) $e^x \tan x + c$ (D) $e^x \cot x + c$
18	If $f(x) = \sin x + \cos x$ then $f(x)$ is : (A) Even function (B) Odd function (C) Neither even nor odd (D) Constant function
19	$\int_0^3 \frac{1}{9 + x^2} dx = :$ (A) $\frac{\pi}{4}$ (B) $\frac{-\pi}{12}$ (C) $\frac{-\pi}{4}$ (D) $\frac{\pi}{12}$
20	$\frac{d}{dx} (f(x) \sin x) = :$ (A) $f(x) \cos x + f'(x) \sin x$ (B) $f'(x) \sin x - f(x) \cos x$ (C) $f'(x) \cos x$ (D) $f'(x) \cos x + f(x) \sin x$

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(Academic Sessions 2019 – 2021 to 2021 – 2023)

MATHEMATICS

223-1st Annual-(INTER PART – II)

Time Allowed : 2.30 hours

PAPER – II (Essay Type)

GROUP – II

Maximum Marks : 80

SECTION – I

C/H/2-12-2-23

2. Write short answers to any EIGHT (8) questions :

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- (i) Find the domain and range of $f(x) = \sqrt{x^2 - 4}$
- (ii) Show that $x = a \sec \theta$, $y = b \tan \theta$ represents the equation of hyperbola.
- (iii) If $f(x) = -2x + 8$, find $f^{-1}(x)$ and $f^{-1}(-1)$
- (iv) Differentiate $(3 - x)(x - 5)$ w.r.t 'x'
- (v) Find derivative of $\sqrt{\frac{1+x}{1-x}}$
- (vi) If $y = x^4 + 2x^2 + 2$, prove $\frac{dy}{dx} = 4x\sqrt{y-1}$
- (vii) Find the derivative of $(x^3 + 1)^9$ w.r.t. 'x'
- (viii) Find $\frac{dy}{dx}$ if $y^3 - 2xy^2 + x^2y + 3x = 0$
- (ix) Differentiate w.r.t. variable involved of $\tan^3 \theta \sec^2 \theta$
- (x) Find $\frac{dy}{dx}$ if $y = a^x$
- (xi) Define feasible region.
- (xii) Graph the feasible region $2x - 3y \leq 6$, $x \geq 0$, $y \geq 0$

3. Write short answers to any EIGHT (8) questions :

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- (i) Using differentials to find $\frac{dy}{dx}$ if $xy - \ln x = c$
- (ii) Evaluate $\int \left(\sqrt{x} + \frac{1}{\sqrt{x}} \right) dx$
- (iii) Evaluate $\int \frac{e^x}{e^x + 3} dx$
- (iv) Evaluate $\int \ln x dx$
- (v) Evaluate $\int_{-6}^2 \sqrt{3-x} dx$
- (vi) Find the area bounded by cos function from $x = -\frac{\pi}{2}$ to $x = \frac{\pi}{2}$
- (vii) Solve the differential equation $\sec^2 x \tan y dx + \sec^2 y \tan x dy = 0$
- (viii) Find the magnitude of the vector $\vec{u} = \hat{i} + \hat{j}$
- (ix) Find direction cosines of $\vec{v} = 3\hat{i} - \hat{j} + 2\hat{k}$
- (x) Calculate the projection of \vec{b} along \vec{a} if $\vec{a} = \hat{i} - \hat{k}$; $\vec{b} = \hat{j} + \hat{k}$
- (xi) If $\vec{a} = 2\hat{i} + \hat{j} - \hat{k}$; $\vec{b} = \hat{i} - \hat{j} + \hat{k}$, find $\vec{b} \times \vec{a}$
- (xii) Prove that the vectors $\hat{i} - 2\hat{j} + 3\hat{k}$, $-2\hat{i} + 3\hat{j} - 4\hat{k}$ and $\hat{i} - 3\hat{j} + 5\hat{k}$ are coplanar.

(Turn Over)

4. Write short answers to any NINE (9) questions :

- (i) Find the equation of the straight line whose slope is 2 and y-intercept is 5.
- (ii) Using slopes, show that the triangle with its vertices A (6, 1), B (2, 7) and C (- 6, - 7) is a right triangle.
- (iii) Find an equation of the line through (- 4, 7) and parallel to the line $2x - 7y + 4 = 0$
- (iv) Find h such that A (- 1, h), B (3, 2) and C (7, 3) are collinear.
- (v) Write intercepts form of equation of straight line.
- (vi) Check whether the following lines are concurrent or not
 $3x - 4y - 3 = 0$
 $5x + 12y + 1 = 0$
 $32x + 4y - 17 = 0$
- (vii) Find the slope and inclination of the line joining points (- 2, 4) and (5, 11)
- (viii) Find an equation of circle with centre at $(\sqrt{2}, -3\sqrt{3})$ and radius $2\sqrt{2}$
- (ix) Define focus and directrix of the parabola.
- (x) Find the centre and foci of the ellipse $x^2 + 4y^2 = 16$
- (xi) Find equation of tangent to $y^2 = 4ax$ at (x_1, y_1)
- (xii) Show that the equation $5x^2 + 5y^2 + 24x + 36y + 10 = 0$ represents a circle. Find its centre.
- (xiii) Find an equation of the ellipse with given data : Foci (0, - 1) and (0, - 5) and major axis of length 6.

SECTION - II

Note : Attempt any THREE questions.

5. (a) If θ is measured in radians then prove that $\lim_{\theta \rightarrow 0} \frac{\sin \theta}{\theta} = 1$ 5
- (b) Find $\frac{dy}{dx}$ if $y = (1 + 2\sqrt{x})^3 \cdot x^{\frac{3}{2}}$ 5
6. (a) Evaluate $\int \ln(x + \sqrt{x^2 + 1}) dx$ 5
- (b) Find equations of two parallel lines perpendicular to $2x - y + 3 = 0$ such that the product of the x-intercept and y-intercept of each is 3. 5
7. (a) Solve the differential equation $2e^x \tan y dx + (1 - e^x) \sec^2 y dy = 0$ 5
- (b) Maximize $f(x, y) = x + 3y$ subject to constraints
 $2x + 5y \leq 30$, $5x + 4y \leq 20$, $x \geq 0$, $y \geq 0$ 5
8. (a) If $y = e^x \sin x$, show that $\frac{d^2y}{dx^2} - 2\frac{dy}{dx} + 2y = 0$ 5
- (b) Find equations of tangents to the circle $x^2 + y^2 = 2$ perpendicular to the line $3x + 2y = 6$ 5
9. (a) Show that the equation $9x^2 - 18x + 4y^2 + 8y - 23 = 0$ represents an ellipse. Find its elements and sketch its graph. 5
- (b) Prove that in any triangle ABC $c = a \cos B + b \cos A$ 5