GROUP: SECOND DAL-12-2-3 OBJECTIVE MARKS: 20 NOTE: You have four choices for each objective type question as A, B, C and D. The choice which you think is correct, fill that circle in front of that question number. Use marker or pen to fill the circles. Cutting or filling two or more circles will result in zero mark in that question.

QUESTION NO. 1

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\frac{d}{dx} \left[ \frac{f(x)}{g(x)} \right] =
(A) \frac{f(x)g'(x) - f'(x)g(x)}{[g(x)]^2} \ (B) \ \frac{f^{'}(x)g(x) - g'(x)f(x)}{[f(x)]^2} \ (C) \ \frac{g(x) \, f^{'}(x) - f(x)g^{'}(x)}{[g(x)]^2} \ (D) \frac{g'(x) \, f'(x) - f(x)g(x)}{[g(x)]^2}
\frac{1}{1+x^2} is derivation of
(A) \sin^{-1} x (B) \sec^{-1} x (C) \tan^{-1} x (D) \cot^{-1} x
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3 $\int ln x dx$ is equal to

$$\int \ln x \, dx \quad \text{is equal to}$$
(A) $x - x \ln x + c$ (B) $x \ln x + x + c$ (C) $\frac{1}{x} \ln x + c$ (D) $x \ln - x + c$

$$4 \int_{1}^{3} (x^2 + 1) \ dx =$$

$$\int_{1}^{1} (x^{2} + 1) dx =$$
(A) $\frac{3}{10}$ (B) 2 (C) $\frac{10}{3}$ (D) 0

$$\int a^x dx =$$

$$\int a^{x} dx = \frac{1}{(A) \frac{a^{x}}{\ln a} + c} \qquad (B) \frac{\ln a}{a^{x}} + c \qquad (C) \frac{1}{a^{x} \ln a} + c \qquad (D) a^{x} \ln a + c$$
The solution of differential equation $\frac{dy}{dx} = -y$ is
$$(A) y = x e^{-x} \qquad (B) y = c e^{-x} \qquad (C) y = e^{x} \qquad (D) y = e^{x}$$
The solution of the solution

The distance between the points
$$(0, 0)$$
 and $(1, 2)$ is

7

(A) 0 (B) 1 (C) 2 (D)
$$\sqrt{5}$$

8 A linear equation in two variables represents

(A) circle (B) ellipse (C) hyperbola (D) straight line

The slope- intercept form of equation of line is

(A)
$$y = \frac{1}{m}x - c$$
 (B) $y = mx + c$ (C) $y = cx + m$ (D) $y = cx - m$

Bisectors of angles of a triangle are 10

(C) Concurrent (D) Non-concurrent (B) Perpendicular

11 The feasible solution which maximizes or minimizes the objective function is called (A) Exact solution (B) Final solution (C) Optimal solution (D) Objective solution

Equation of circle with centre at origin and radius $\sqrt{5}$ is 12

(A)
$$x^2 + y^2 = \sqrt{5}$$
 (B) $x^2 + y^2 = 5$ (C) $x^2 + y^2 = 25$ (D) $(x - 3)^2 + y^2 = 5$

13 The parabola $y^2 = 4ax$, a > 0 opens

(D) Downward (A) Right (B) Left (C) Upward

In an ellipse, the foci lie on (A) Major axis (B) Minor axis (C) Directin (D) Z – axis If $\overline{F} = 4i + 3j + 5k$ and $\overline{d} = -i + 3j + 8k$, then work done is

15

(A) 30 unit (B) 45 unit (C) 53 unit (D) 47 unit

If U, V and W are coterminous edges of a tetrahedron, then its volume is 16

(A)
$$[\underline{\underline{U}}\underline{\underline{V}}\underline{\underline{W}}]$$
 (B) $\frac{1}{3}[\underline{\underline{U}}\underline{\underline{V}}\underline{\underline{W}}]$ (C) $\frac{1}{6}[\underline{\underline{U}}\underline{\underline{V}}\underline{\underline{W}}]$ (D) $\frac{1}{9}[\underline{\underline{U}}\underline{\underline{V}}\underline{\underline{W}}]$

If $f(x) = x^2$, then range of f is

(A) All non-negative real numbers (B) Rational numbers (C) Integers (D) Irrational numbers

18

 $\frac{d}{dx}(x^{an}) = 0$

(A)
$$-anx^{an-1}$$
 (B) $) anx^{an-1}$ (C) $(an-1)x^{an-1}$

(C)
$$(an-1)x^{an-1}$$

(D)
$$\frac{x^{an+1}}{an+1}$$

20 If $y = \frac{1}{x^2}$, then $\frac{dy}{dx}$ at x = -1 is

(D) 4 (A) 2 (B) 3 (C) $\frac{1}{2}$

MATHEMATICS

12th CLASS – 1st Annual 2023

GROUP: SECOND

SUBJECTIVE

SECUTION I

TIME: 2.30 HOURS MARKS: 80

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QUESTION NO. 2 Write short answers any Eight (8) of the following

i Prove the identity $sech^2x = 1 - tanh^2x$ ii Evalaute $\lim_{x \to \infty} \left(\frac{x}{1+x}\right)^x$ iii If $f(x) = \begin{cases} x+2, & x \le -1 \\ c+2, & x > -1 \end{cases}$, Find C so that $\lim_{x \to -1} f(x)$ exists

iv Differentiate w.r.t 'x' $\left(\sqrt{x} - \frac{1}{\sqrt{x}}\right)^2$ v Find $\frac{dy}{dx}$, if $x = \theta + \frac{1}{\theta}$ and $y = \theta + 1$ vi Differentiate w.r.t 'x' $\cos \sqrt{x} + \sqrt{\sin x}$ vii Find f(x) if $f(x) = \frac{e^x}{e^{-x} + 1}$ viii Find y_2 if $x = at^2$, $y = bt^4$ ix Apply Maclaurin series expansion to prove $e^{2x} = 1 + 2x + \frac{4x^2}{2!} + \frac{8x^3}{3!} + \dots$ x Find two positive integers whose sum is 30 and their product will be miximum.

QUESTION NO. 3 Write short answers any Eight (8) of the following

xi

Graph the solution region of linear inequality $3x - 2y \ge 6$

Graph the linear inequality $2x \ge -3$ in xy - plane.

Find $\int x \cos x \, dx$ Evaluate $\int x^2 \tan^{-1} x \, dx$ iii Evaluate $\int_{3}^{\frac{\pi}{3}} \cos^2 \theta \sin \theta d\theta$ Evaluate $\int_{1}^{e} x \ln x \, dx$ Find area between the x-axis and the curve $y = 4x - x^2$ vii Solve the differential equation $\sec x + \tan y$ If $\overrightarrow{AB} = \overrightarrow{CD}$. Find coordinates of the point A when points B, C, D are (1, 2), (-2, 5), (4, 11) respectively. Prove $\cos^2 \alpha + \cos^2 \beta + \cos^2 \gamma = 1$ ix Find a vector whose magnitude is 4 and is parallel to $2\underline{i} - 3j + 6\underline{k}$ X Show that the components of a vector are projections of that vectors along \underline{i} , j and \underline{k} respectively. Show that the vectors $3\underline{i} - 2\underline{j} + \underline{k}$, $\underline{i} - 3\underline{j} + 5\underline{k}$ and $2\underline{i} - \underline{j} - 4\underline{k}$ from a right angle triangle.

QUESTION NO. 4 Write short answers any Nine (9) of the following

i Show that for the points A(3,1), B(-2,-3) and C(2,2), $|\overline{AB}| = |\overline{BC}|$

i	Show that for the points $A(3,1)$, $B(-2,-3)$ and $C(2,2)$, $ \overline{AB} = \overline{BC} $
ii	Find the point that divide the join of $A(-6, 3)$ and $B(5, -2)$ in the ratio 2: 3 internally.
iii	Find the slope and inclination of line joining the points (4, 6); (4, 8)
iv	Find an equation of line with x-intercept: -9 and slope: -4
v	Find the area of triangle whose vertices are A $(2,3)$, B $(-1,1)$ and C $(4,-5)$
vi	Find the lines represented by the equation $2x^2 + 3xy - 5y^2 = 0$
vii	Find an equation of the line through $(11, -5)$ and parallel to a line with slope -24
viii	Find an equation of circle with centre $(-3, 5)$ and radius 7
ix	Find centre and radius of circle $x^2 + y^2 - 6x + 4y + 13 = 0$
X.	Check the position of the point (5, 6) w.r.t circle $x^2 + y^2 = 81$
xi	Find an equation of parabola with focus $(-3, 1)$ and directrix $x = 3$
xii	Find centre and foci of the ellipse $x^2 + 4y^2 = 16$
xiii	Find foci and vertices of hyperbola $\frac{y^2}{4} - x^2 = 1$
	- MT

(P.T.O)

SECTION-II

Note: Attempt any Three questions from this section

 $10 \times 3 = 30$

Q.5- (A)	Find the values m and n so that the given function $f(x)$ is continuous at $x = 3$ $f(x) = \begin{cases} mx & \text{if } x < 3 \\ n & \text{if } x = 3 \\ -2x + 9 & \text{if } x > 3 \end{cases}$
(B)	If $y = \sqrt{x} - \frac{1}{\sqrt{x}}$ show that $2x \frac{dy}{dx} + y = 2\sqrt{x}$
Q.6- (A)	Evaluate $\int e^{2x} \cos 3x \ dx$
(B)	Find an equation of the line through (5, -8) and perpendicular to the join of A(-15, -8), B(10,7)
Q.7-(A) (B)	Find the area between the x-axis and the curve $y = \sqrt{2ax - x^2}$, where $a > 0$ Maximize $f(x,y) = x + 3y$ subject to the constraints $2x + 5y \le 30$; $5x + 4y \le 20$; $y \ge 0$
Q.8-(A)	Find y_4 if $y = cos^3 x$
(B)	Find equation of circle passing through A $(3, -1)$, B $(0, 1)$ and having centre at $4x-3y-3=0$
Q.9-(A)	Find the centre, foci eccentricity, vertices and equation of directrices of $\frac{(x-1)^2}{2} - \frac{(y-1)^2}{9} = 1$
(B)	Prove that $C = a \cos B + b \cos A$.

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