GROUP-II

OBJECTIVE

MAXIMUM MARKS: 20

Note: You have four choices for each objective type question as A, B, C and D. The choice which you think is correct, fill that bubble in front of that question number, on bubble sheet. Use marker or pen to fill the bubbles. Cutting or filling two or more bubbles will result in zero mark in that question. No credit will be awarded in case BUBBLES are not filled. Do not solve question on this sheet of OBJECTIVE PAPER.

Q.No.1

(5)

(1) The perimeter
$$P$$
 of a square as a function of its area A is:

$$(A) P = \sqrt{A}$$

(B)
$$P = 2\sqrt{A}$$

(C)
$$P = 3\sqrt{A}$$

(B)
$$P = 2\sqrt{A}$$
 (C) $P = 3\sqrt{A}$ (D) $P = 4\sqrt{A}$

$$\lim_{x \to 3} \frac{x-3}{\sqrt{x} - \sqrt{3}}$$

(A)
$$\sqrt{3}$$

(B)
$$2\sqrt{3}$$

(C)
$$\frac{1}{\sqrt{3}}$$

(A)
$$\sqrt{3}$$
 (B) $2\sqrt{3}$ (C) $\frac{1}{\sqrt{3}}$ (D) $\frac{1}{2\sqrt{3}}$

(3) If
$$3x + 4y - 5 = 0$$
, then $\frac{dy}{dx} =$

(A)
$$\frac{4}{3}$$

(A)
$$\frac{4}{3}$$
 (B) $-\frac{4}{3}$ (C) $\frac{3}{4}$ (D) $-\frac{3}{4}$

(C)
$$\frac{3}{4}$$

(D)
$$-\frac{3}{4}$$

(4)
$$\frac{d}{dx}(\sqrt{\cot x}) =$$

(A)
$$\frac{1}{2\sqrt{\cot x}}$$

(B)
$$\frac{\cos ec^2x}{2\sqrt{\cot x}}$$

(A)
$$\frac{1}{2\sqrt{\cot x}}$$
 (B) $\frac{\cos ec^2x}{2\sqrt{\cot x}}$ (C) $\frac{-\cos ec^2x}{2\sqrt{\cot x}}$ (D) $\frac{2\cos ec^2x}{\sqrt{\cot x}}$

(D)
$$\frac{2\cos ec^2x}{\sqrt{\cot x}}$$

(5) If
$$f(x) = \tan^{-1} x$$
, then $f'(\cot x) =$ (A) $\sin^2 x$ (B) $\cos^2 x$ (C) $\sec^2 x$ (D) $\frac{1}{1+x^2}$
(6) $\frac{d}{dx}(-\cot x) =$ (A) $\sec^2 x$ (B) $\csc^2 x$ (C) $-\csc^2 x$ (D) $\tan^2 x$

$$(\Delta) \sec^2 r$$

(A)
$$\sec^2 x$$
 (B) $\cos ec^2 x$ (C) $-\cos ec^2 x$ (D) $\tan^2 x$

$$(D) \tan^2 x$$

(7)
$$\int a^x dx =$$

(A)
$$a^x + c$$

(B)
$$a^x + \ell na + \epsilon$$

(A)
$$a^x + c$$
 (B) $a^x + \ln a + c$ (C) $a^x \cdot \ln a + c$ (D) $a^x \cdot \frac{1}{\ln a} + c$

(D)
$$a^x \cdot \frac{1}{\theta_{n\alpha}} +$$

(8) The anti-derivative of
$$\frac{1}{(1+x^2)\tan^{-1}x}$$
 is:

(A)
$$\ln(\tan^{-1}x) + c$$

(B)
$$\ln(1+x^2) + \epsilon$$

(C)
$$2(\tan^{-1}x)^2 +$$

(B)
$$\ln(1+x^2) + c$$
 (C) $2(\tan^{-1}x)^2 + c$ (D) $\frac{1}{2}(\tan^{-1}x)^2 + c$

(9) Suitable substitution for solving
$$\int \frac{1}{x\sqrt{x^2-a^2}} dx$$
 is:

(A)
$$x = a \sin \theta$$

(B)
$$x = a \tan \theta$$
 (C) $x = a \sec \theta$

(C)
$$x = a \sec \theta$$

(D)
$$x = a \cos \theta$$

$$(10) \qquad \int_0^{\pi/4} \sec^2 x \ dx =$$

$$(C)$$
 2

(D)
$$\frac{1}{2}$$

(12) The point
$$(3, -8)$$
 lies in the quadrant.

$$3^{rd}$$
 (D) 4^{th}

(13) The lines
$$\ell_1$$
 and ℓ_2 with slopes m_1 and m_2 respectively, are parallel if:

(A)
$$m_1 m_2 = 1$$

(B)
$$m_1 = m_2$$

(C)
$$m_1 m_2 = -1$$

(D)
$$m_1 + m_2 = 0$$

$$(A) 2x + y > 3$$

(B)
$$2x + y > 4$$

(C)
$$2x + y < 1$$

(D)
$$2x + y > 1$$

(15) Centre of the circle
$$x^2 + y^2 + 7x - 3y = 0$$
, is:

(A)
$$(7, -3)$$

(B)
$$\left(-\frac{7}{2}, \frac{3}{2}\right)$$
 (C) $(-7, 3)$

$$(C)(-7,3)$$

(D)
$$(\frac{7}{2}, -\frac{3}{2})$$

(16) The equation of directrix of the parabola
$$x^2 = 5y$$
 is:

(A)
$$x + \frac{5}{4} = 0$$

(B)
$$x - \frac{5}{4} = 0$$

(B)
$$x - \frac{5}{4} = 0$$
 (C) $y + \frac{5}{4} = 0$

(D)
$$y - \frac{5}{4} = 0$$

(17) The length of latus-rectum of hyperbola
$$\frac{x^2}{a^2} - \frac{y^2}{b^2} = 1$$
, is:

(A)
$$\frac{a^2}{2b}$$

(B)
$$\frac{b^2}{2a}$$

(C)
$$\frac{b^4}{a}$$

(D)
$$\frac{2b^2}{a}$$

(18) If
$$\underline{u} = 2\alpha \underline{i} + \underline{j} - \underline{k}$$
 and $\underline{v} = \underline{i} + \alpha \underline{j} + 4\underline{k}$, are perpendicular, then $\alpha =$

(A)
$$-\frac{4}{3}$$

(B)
$$\frac{4}{3}$$

(C)
$$\frac{3}{4}$$

(19) The vectors
$$u$$
, \underline{v} and \underline{w} are coplanar if:

(A)
$$\underline{u} \cdot \underline{v} \times \underline{w} = 0$$

(B)
$$\underline{u} \cdot \underline{v} \times \underline{w} = 1$$

(C)
$$\underline{u} \cdot \underline{v} \times \underline{w} = 2$$

(D)
$$\underline{u} \cdot \underline{v} \times \underline{w} = 3$$

(20) Work done by a constant force
$$\vec{F}$$
 during a displacement \vec{d} is equal to:

(A)
$$\vec{F} \times \vec{d}$$

(B)
$$\vec{d} \times \vec{F}$$

(C)
$$\vec{F} + \vec{d}$$

$$+ \vec{d}$$

(D)
$$\vec{F} \cdot \vec{d}$$

NOTE: Write same question number and its part number on answer book, as given in the question paper.

SECTION-I

2. Attempt any eight parts.

 $8\times2=16$

(i) Express perimeter P of a square as a function of its area A.

(ii) If
$$f(x) = \sqrt{x+1}$$
, $g(x) = \frac{1}{x^2}$ find $f \circ g(x)$, $g \circ f(x)$

- (iii) Evaluate $\lim_{x \to -1} \frac{x^3 x}{x + 1}$
- (iv) Evaluate $\lim_{x \to 0} \frac{1 \cos x}{\sin^2 x}$
- (v) Differentiate $\left(\sqrt{x} \frac{1}{\sqrt{x}}\right)^2$ w.r.t. x
- (vi) Find $\frac{dy}{dx}$ if $x = 1 t^2$, $y = 3t^2 2t^3$
- (vii) Prove that $\frac{d}{dx}(\tan^{-1} x) = \frac{1}{1+x^2}$
- (viii) Find $\frac{dy}{dx}$ if $y = x \cos y$
- (ix) Find $\frac{dy}{dx}$ if $y = \frac{x}{\ell nx}$
- (x) Find f'(x) if $f(x) = e^{\sqrt{x-1}}$
- (xi) Find y_2 if $y = x^2 e^{-x}$
- (xii) Find Maclaurin series for $\sin x$.

3. Attempt any eight parts.

 $8 \times 2 = 16$

- (i) Use differentials to find dy and δy if $y = x^2 + 2x$, x changes from 2 to 1.8.
- (ii) Find $\int \frac{1-\sqrt{x}}{\sqrt{x}} dx$
- (iii) Find $\int_{1+x^2}^{1-x^2} dx$
- (iv) Find $\int \frac{\cot \sqrt{x}}{\sqrt{x}} dx$
 - (v) Find $\int \frac{\sqrt{2}}{\sin x + \cos x} dx$
 - (vi) Find $\int x \, \ell nx \, dx$
 - (vii) Solve the differential equation $(e^x + e^{-x}) \frac{dy}{dx} = e^x e^{-x}$
 - (viii) Find $\int_{0}^{\pi/3} \cos^2 \theta \sin \theta \ d\theta$
 - (ix) By means of slope, show that (-1, -3), (1, 5), (2, 9) lie on the same line.
 - (x) Check whether the point (-7, 6) lies above or below the line 4x + 3y 9 = 0
 - (xi) Check whether the lines 12x + 35y 7 = 0 and 105x 36y + 11 = 0 are parallel or perpendicular.
- (xii) Express 15y 8x + 3 = 0 in normal form.

- (i) Graph the solution set of $3x 2y \ge 6$
- (ii) Find an equation of the circle with ends of a diameter at (-3, 2) and (5, -6)
- (iii) Find the radius of the circle $5x^2 + 5y^2 + 14x + 12y 10 = 0$
- (iv) Find the length of the tangent drawn from the point (-5, 4) to the circle $5x^2 + 5y^2 10x + 15y 131 = 0$
- (v) Find the focus and directrix of the parabola $x^2 = 4(y-1)$
- (vi) Find the foci and eccentricity of $\frac{y^2}{16} \frac{x^2}{9} = 1$
- (vii) Write down the equation of tangent to $3x^2 + 3y^2 + 5x 13y + 2 = 0$ at $\left(1, \frac{10}{3}\right)$
- (viii) Find the magnitude of the vector $\vec{u} = \hat{i} + \hat{j}$
- (ix) Find a unit vector in the direction of $\underline{v} = 2\underline{i} \underline{j}$
- (x) Let $\underline{v} = 3\underline{i} 2\underline{j} + 2\underline{k}$, $\underline{w} = 5\underline{i} \underline{j} + 3\underline{k}$ find $\underline{v} 3\underline{w}$
- (xi) Find α so that $\left| \alpha \underline{i} + (\alpha + 1) \underline{j} + 2\underline{k} \right| = 3$
- (xii) Find the direction cosines of $\underline{v} = 3\underline{i} j + 2\underline{k}$
- (xiii) Find a vector of lengths 5 in the direction opposite that of $\underline{v} = \underline{i} 2\underline{j} + 3\underline{k}$

SECTION-II

NOTE: Attempt any three questions.

$$3 \times 10 = 30$$

- 5.(a) Prove that $y \frac{dy}{dx} + x = 0$ if $x = \frac{1 t^2}{1 + t^2}$, $y = \frac{2t}{1 + t^2}$
 - (b) If $f(x) = \begin{cases} \frac{\sqrt{2x+5} \sqrt{x+7}}{x-2} & x \neq 2 \\ K & x=2 \end{cases}$ find value of K so that f is continuous at x=2
- 6.(a) Determine value of p such that the lines 2x 3y 1 = 0, 3x y 5 = 0 and 3x + py + 8 = 0 meet at a point.
 - (b) Evaluate $\int x^3 e^{5x} dx$
- 7. (a) Evaluate $\int_{-1}^{2} (x + |x|) dx$
 - (b) Minimize z = 2x + y; subject to the constraints $x + y \ge 3$; $7x + 5y \le 35$; $x \ge 0$, $y \ge 0$
- 8. (a) Show that the circles $x^2 + y^2 + 2x 2y 7 = 0$ and $x^2 + y^2 6x + 4y + 9 = 0$ touch externally.
 - (b) A force of magnitude 6 units acting parallel to $2\underline{i} 2\underline{j} + \underline{k}$, displaces, the point of application from (1, 2, 3) to (5, 3, 7). Find work done.
- 9.(a) A box with a square base and open top is to have a volume of 4 cubic *dm*. Find the dimensions of the box which will require the least material.
 - (b) Find the centre, foci and vertices of the following $9x^2 12x y^2 2y + 2 = 0$