

Roll No \_\_\_\_\_ (To be filled in by the candidate)

(Academic Sessions 2017 – 2019 to 2019 – 2021)

MATHEMATICS

221-(INTER PART – II)

Time Allowed : 30 Minutes

Q.PAPER – II ( Objective Type )

GROUP – II

Maximum Marks : 20

PAPER CODE = 8198

Note : Four possible answers A, B, C and D to each question are given. The choice which you think is correct, fill that circle in front of that question with Marker or Pen ink in the answer-book. Cutting or filling two or more circles will result in zero mark in that question.

1-1	The derivative of $\frac{1}{1+x}$ is : (A) $x$ (B) $1+x$ (C) $(1+x)^{-2}$ (D) $-1(1+x)^{-2}$
2	$\int \cos x \, dx = :$ (A) $1 - \sin^2 x$ (B) $\sqrt{1 - \sin^2 x}$ (C) $\sin x$ (D) $-\sin x$
3	$\int_1^2 (x^2 + 1) \, dx = :$ (A) $\frac{10}{3}$ (B) $\frac{3}{10}$ (C) $\pi$ (D) $\frac{\pi}{2}$
4	If $y = \cot^{-1} x$ , then $\frac{dy}{dx} = :$ (A) $\frac{1}{1-x^2}$ (B) $\frac{-1}{1+x^2}$ (C) $\frac{1}{x^2+1}$ (D) $\frac{1}{x^2+1}$
5	The derivative of $\ln(\tanh x)$ is : (A) $\frac{1}{\tanh x}$ (B) $\frac{\sec^2 x}{\tanh x}$ (C) $\sec^2 x$ (D) $\sec x$
6	$x = at^2$ and $y = 2at$ are parametric equations of : (A) Parabola (B) Ellipse (C) Circle (D) Hyperbola
7	If $y^2 + x^2 = a^2$ , then $\frac{dy}{dx} = :$ (A) $-\frac{x}{y}$ (B) $-\frac{y}{x}$ (C) $\frac{x}{y}$ (D) $\frac{y}{x}$
8	The order of $\frac{dy}{dx} = \frac{4}{3}x^3 + x - 3$ is : (A) 1 (B) $\frac{3}{4}$ (C) $\frac{4}{3}$ (D) $-3$
9	$\int_a^x 3x^2 \, dx = :$ (A) $x^3 + a^3$ (B) $x^3 - a^3$ (C) $3x^3$ (D) $x^3$

( Turn Over )

1-10	<p>If <math>\theta</math> is measured in radian then <math>\lim_{\theta \rightarrow 0} \frac{\sin 7\theta}{\theta} = :</math></p> <p>(A) 7 (B) <math>\frac{1}{7}</math> (C) <math>\frac{7\pi}{22}</math> (D) <math>\frac{7\pi}{12}</math></p>
11	<p>The measure of the angle between the lines <math>ax^2 + 2hxy + by^2 = 0</math> is given by <math>\tan \theta = :</math></p> <p>(A) <math>\frac{\sqrt{h^2 - ab}}{a - b}</math> (B) <math>\frac{2\sqrt{h^2 - ab}}{a + b}</math> (C) <math>\frac{h^2 - ab}{a + b}</math> (D) <math>\infty</math></p>
12	<p>If <math>\vec{a} = \hat{i} - \hat{j}</math> and <math>\vec{b} = \hat{j} + \hat{k}</math> then <math>\vec{a} \cdot \vec{b} = :</math></p> <p>(A) 0 (B) 1 (C) -1 (D) <math>\sqrt{2}</math></p>
13	<p>The feasible solution which maximize or minimize the objective function is called :</p> <p>(A) Boundary (B) Half plane (C) Optimal solution (D) Initial values</p>
14	<p>The value of c for <math>\frac{y^2}{16} - \frac{x^2}{49} = 1</math> is :</p> <p>(A) 16 (B) 49 (C) 65 (D) <math>\sqrt{65}</math></p>
15	<p>The equation of a straight line represented by <math>x \cos \alpha + y \sin \alpha = P</math> is called :</p> <p>(A) Normal form (B) Angular form (C) Symmetric form (D) P - form</p>
16	<p>The unit vector in the direction of <math>\vec{v} = [3, -4]</math> :</p> <p>(A) <math>5[3, -4]</math> (B) <math>\frac{1}{5}[3, -4]</math> (C) <math>\hat{i}</math> (D) <math>\hat{j}</math></p>
17	<p>The points A <math>(-5, -2)</math>, B <math>(5, 4)</math> are ends point of a diameter of the circle. The centre will be :</p> <p>(A) <math>(0, 3)</math> (B) <math>(0, -3)</math> (C) <math>(5, 2)</math> (D) <math>(-5, 4)</math></p>
18	<p><math>xy = 0</math> represents :</p> <p>(A) A pair of lines (B) Hyperbola (C) Parabola (D) Ellipse</p>
19	<p>The projection of <math>\vec{v}</math> along <math>\vec{u}</math> is :</p> <p>(A) <math>\frac{\vec{u} \cdot \vec{v}}{ \vec{u} }</math> (B) <math>\frac{\vec{u} \cdot \vec{v}}{ \vec{v} }</math> (C) <math>\frac{\vec{u} \cdot \vec{v}}{ \vec{u}   \vec{v} }</math> (D) <math>\frac{\vec{u} \cdot \vec{v}}{ \vec{u}  +  \vec{v} }</math></p>
20	<p>An angle inscribed in a semi-circle is :</p> <p>(A) 0 (B) <math>\frac{\pi}{2}</math> (C) <math>\pi</math> (D) <math>2\pi</math></p>

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(Academic Sessions 2017 – 2019 to 2019 – 2021)

MATHEMATICS

221-(INTER PART – II)

PAPER – II (Essay Type)

GROUP – II

Time Allowed : 2.30 hours

Maximum Marks : 80

## SECTION – I

## 2. Write short answers to any EIGHT (8) questions :

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- (i) Express the area  $A$  of a circle as a function of its circumference  $C$ .
- (ii) For the real-valued function  $f(x) = \frac{2x+1}{2x-1}$ ,  $x > 1$ . Find  $f^{-1}(x)$
- (iii) Evaluate  $\lim_{x \rightarrow 3} \frac{x-3}{\sqrt{x}-\sqrt{3}}$
- (iv) Find the domain and range of  $g(x) = |x-3|$
- (v) If  $y = \left( \sqrt{x} - \frac{1}{\sqrt{x}} \right)^2$ , find  $\frac{dy}{dx}$
- (vi) Find  $\frac{dy}{dx}$  if  $xy + y^2 = 2$
- (vii) Differentiate  $\sin x$  w.r.t.  $\cot x$
- (viii) Find  $\frac{dy}{dx}$  if  $y = x^2 \ln \frac{1}{x}$
- (ix) Find  $y_2$  if  $y = x^2 \cdot e^{-x}$
- (x) If  $y = \ln(\tanh x)$ , find  $\frac{dy}{dx}$
- (xi) Find  $\frac{dy}{dx}$  if  $y = (x^2 + 5)(x^3 + 7)$
- (xii) Find  $f'(x)$  if  $f(x) = \sqrt{\ln(e^{2x} + e^{-2x})}$

## 3. Write short answers to any EIGHT (8) questions :

16

- (i) Use differential to find  $\frac{dy}{dx}$  for  $xy + x = 4$
- (ii) Evaluate the integral  $\int \frac{3x+2}{\sqrt{x}} dx$
- (iii) Evaluate  $\int \frac{x+b}{(x^2+2bx+c)^{1/2}} dx$
- (iv) Evaluate  $\int e^x (\cos x + \sin x) dx$
- (v) Evaluate  $\int \frac{(a-b)x}{(x-a)(x-b)} dx$
- (vi) Evaluate  $\int_{-1}^1 (x^{1/3} + 1) dx$
- (vii) Find the area above the x-axis and under the curve  $y = 5 - x^2$  from  $x = -1$  to  $x = 2$
- (viii) Solve differential equation  $ydx + xdy = 0$
- (ix) Find mid-point of line segment joining  $A(-8, 3)$ ;  $B(2, -1)$
- (x) Two points 'P' and 'O' given in xy-coordinate system. Find XY-coordinates of 'P' referred to translated axis  $O'X$  and  $O'Y$  for  $P(-2, 6)$ ;  $O'(-3, 2)$
- (xi) Find equation of the line joining  $(-5, -3)$  and  $(9, -1)$
- (xii) Find equation of vertical line through  $(-5, 3)$

(Turn Over)

## 4. Write short answers to any NINE (9) questions :

- (i) Graph the solution set of given linear inequality in xy-plane :  $2x + y \leq 6$
- (ii) Find the centre and radius of the circle with the given equation  
 $5x^2 + 5y^2 + 14x + 12y - 10 = 0$
- (iii) Find the focus and vertex of the parabola  $x^2 = -16y$
- (iv) Write an equation of parabola with given elements : Focus  $(-3, 1)$  ;  
 directrix  $x - 2y - 3 = 0$
- (v) Find an equation of directrices of given hyperbola  $\frac{x^2}{4} - \frac{y^2}{9} = 1$
- (vi) Find the centre and eccentricity of given hyperbola  $\frac{y^2}{16} - \frac{x^2}{9} = 1$
- (vii) Find the unit vector in the same direction as the vector  $\underline{v} = [3, -4]$
- (viii) Find the constant  $a$  so that the vectors  $\underline{v} = i - 3j + 4k$  and  $\underline{w} = ai + 9j - 12k$  are parallel.
- (ix) Find a vector of length 2 in the direction opposite that of  $\underline{v} = -i + j + k$
- (x) Find the cosine of the angle  $\theta$  between  $\underline{u}$  and  $\underline{v}$   $\underline{u} = [2, -3, 1]$  and  $\underline{v} = [2, 4, 1]$
- (xi) Compute  $\underline{b} \times \underline{a}$ . Check your answer by showing that  $\underline{b}$  is perpendicular to  $\underline{b} \times \underline{a}$  :  
 $\underline{a} = 2i + j - k$  ;  $\underline{b} = i - j + k$ .
- (xii) If  $\underline{a} + \underline{b} + \underline{c} = 0$ , then prove that  $\underline{a} \times \underline{b} = \underline{b} \times \underline{c} = \underline{c} \times \underline{a}$
- (xiii) Give a force  $\underline{F} = 2i + j - 3k$  acting at a point A  $(1, -2, 1)$ . Find the moment of  $\underline{F}$  about the point B  $(2, 0, -2)$

## SECTION - II

Note : Attempt any THREE questions.

5. (a) Find value of  $k$ , if the function  $f(x) = \begin{cases} \frac{\sqrt{2x+5} - \sqrt{x+7}}{x-2}, & x \neq 2 \\ k, & x = 2 \end{cases}$  is continuous at  $x = 2$  5
- (b) If  $y = \tan(p \tan^{-1} x)$  then show that  $(1+x^2)y_1 - p(1+y^2) = 0$  5
6. (a) Evaluate  $\int \frac{\sqrt{2}}{\sin x + \cos x} dx$  5
- (b) Find an equation of the line through the intersection of the lines  $x - y - 4 = 0$  and  $7x + y + 20 = 0$  and parallel to the line  $6x + y - 14 = 0$  5
7. (a) Find the area bounded by the curve  $y = x^3 - 4x$  and the x-axis. 5
- (b) Maximize  $f(x, y) = 2x + 5y$  subject to the constraints  $2y - x \leq 8$ ,  $x - y \leq 4$ ,  $x \geq 0$ ,  $y \geq 0$  5
8. (a) Write equation of the circle passing through the points A  $(-7, 7)$ , B  $(5, -1)$  and C  $(10, 0)$  5
- (b) Find a vector of length 5 in the direction opposite that of  $\underline{v} = i - 2j + 3k$  5
9. (a) Show that  $y = \frac{\ln x}{x}$  has maximum value at  $x = e$  5
- (b) Find focus, vertex and directrix of parabola  $x^2 - 4x - 8y + 4 = 0$  5